

Extracting large- x structure functions (and LHC connections)

Alberto Accardi

Hampton U. and Jefferson Lab

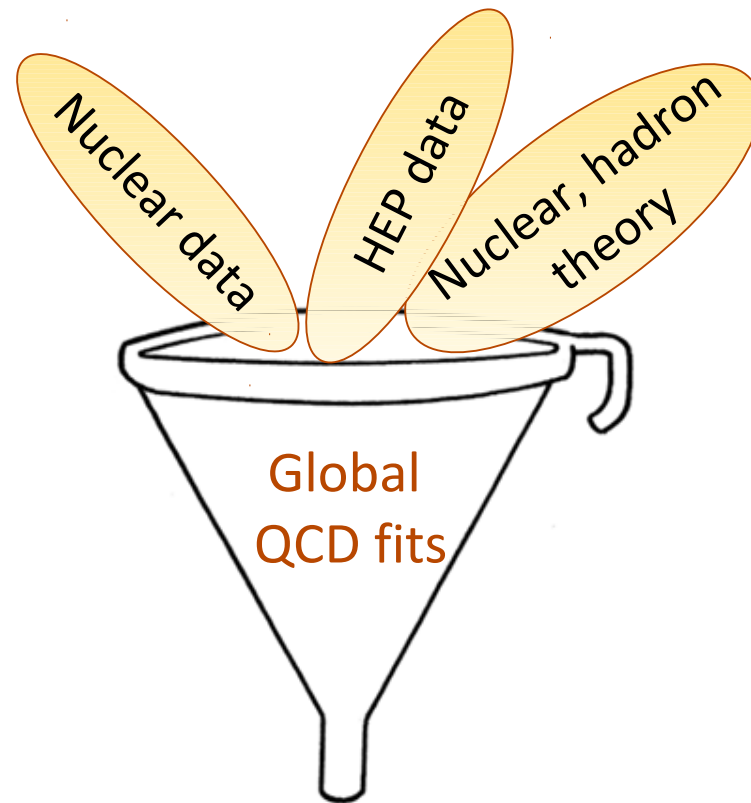
Gordon Research Conference
on “Photonuclear Reactions”
August 5-10, 2012

“The coherence provided by QCD means that insights [into hadron structure] may arise from unexpected quarters.

It is more than ever advisable to take a broad view that integrates across hadronic physics, and to connect with the rest of subatomic physics.”

C. Quigg, 2011

“The Future of Hadrons: The Nexus of Subatomic Physics”
Talk at “Hadron 2011”, arXiv:1109.5814



In-medium nucleons

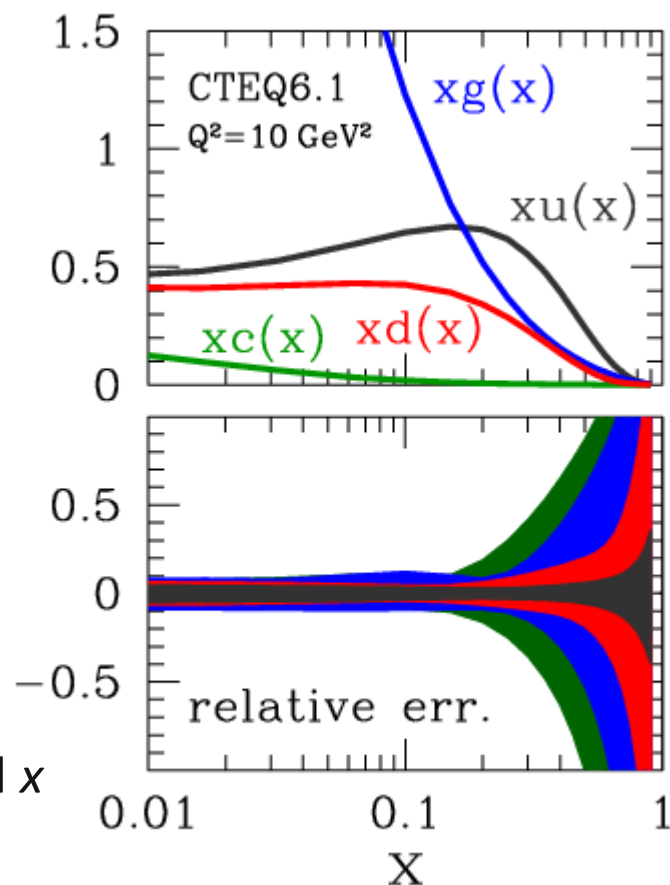
New physics

Why large x ?

□ Large (experimental) uncertainties in Parton Distribution Functions (PDFs)

□ Precise PDFs at large x are needed, *e.g.*,

- Non-perturbative nucleon structure:
 - $d/u, \Delta u/u, \Delta d/d$ at $x \rightarrow 1$
- at LHC, Tevatron
 - New physics as excess on QCD
 - large p_T spectra \Leftrightarrow large x PDF
 - Forward physics
- At RHIC:
 - Spin structure of the nucleon at small x
- Neutrino oscillations, ...



Valence quarks at large x

- At large x , valence u and d extracted from p and n DIS structure functions

$$F_2^p \approx \frac{4}{9}u_v + \frac{1}{9}d_v$$

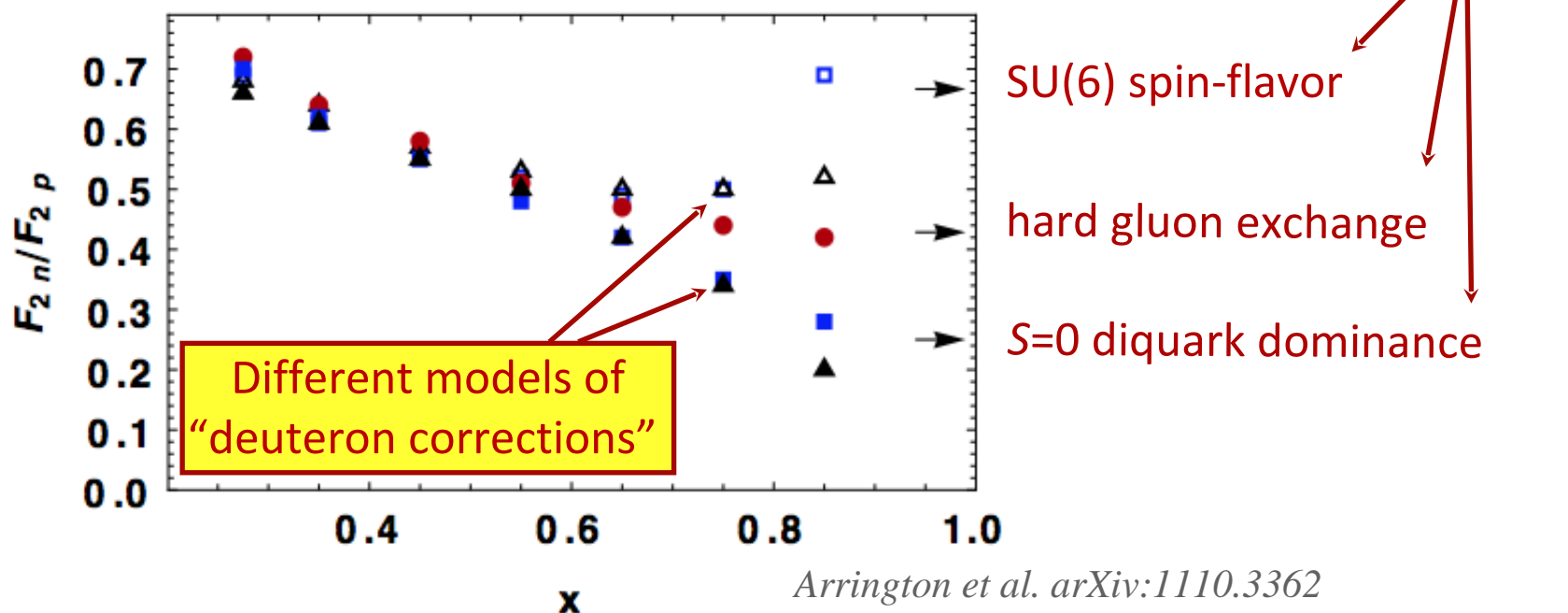
$$F_2^n \approx \frac{1}{9}u_v + \frac{4}{9}d_v$$

- u quark distribution well determined from proton data
- d quark distribution requires neutron structure function

$$\frac{d}{u} \approx \frac{4 - F_2^n / F_2^p}{4F_2^n / F_2^p - 1}$$

But... deuteron corrections!

- Absence of free neutron targets
⇒ use deuterons (weakly bound p and n)



- Deuteron model dependence obscures free neutron at large x
 - We will see quantitatively how much

Large x at colliders - new physics searches

Remember, $x = \frac{M}{\sqrt{s}} e^y$

Examples:

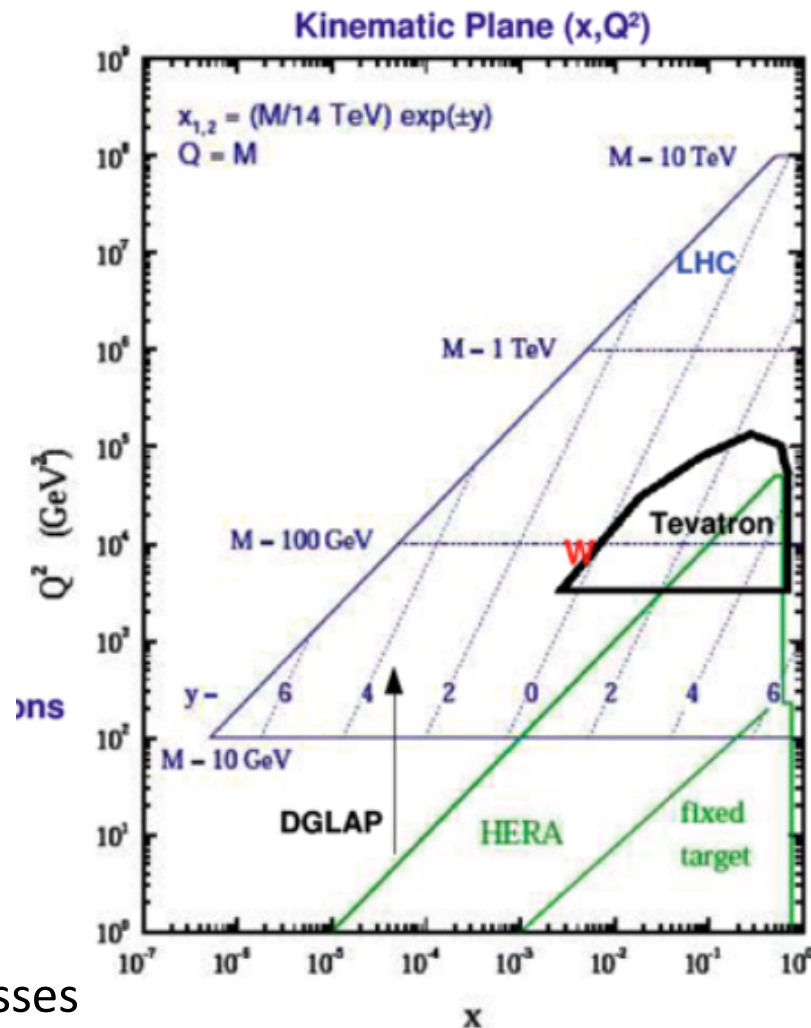
- Z' production $M'_Z \gtrsim 1 \text{ TeV}$
- Higgs at forward rapidity: $y > 2$

$$x > 0.1 \text{ (LHC)}$$

$$x > 0.5 \text{ (Tevatron)}$$

Precise large-x PDFs needed to:

- reduce QCD background
- optimize searches involving large masses
- precisely characterize new particle properties



The CTEQ-JLab fits

The CTEQ-JLab collaboration

□ Collaborators:

- A.Accardi, E.Christy, C.Keppel, W.Melnitchouk, P.Monaghan, J.Owens (J.Morfín, L.Zhu)

□ Goals:

- Global QCD fits of unpolarized PDFs focused on large x
- Improve the PDF experimental precision (“PDF errors”) by enlarging the fitted data set
- Include all relevant large- x / small- Q^2 theory corrections
- *Quantitatively evaluate theoretical systematic errors*
- *Use PDFs as tools for nuclear and particle physics*

□ Papers:

- A.Accardi et al., Phys.Rev.D81 (2010) 034016 **“CJ10”**
- A.Accardi et al., Phys.Rev.D84 (2011) 014008 **“CJ11”**

Global QCD fits of Parton Distribution Functions

data

- DIS: p, d
- $p+p(\bar{p}) \rightarrow l^+l^-, W^\pm$
- $p+p(\bar{p}) \rightarrow \text{jets}, \gamma+\text{jet}$

theory

- pQCD at NLO
- Factorization & universality
- Large- x , low- Q^2 , nuclear corr.

fits

- Parametrize PDF at Q_0 , evolve to Q
- Minimize χ^2

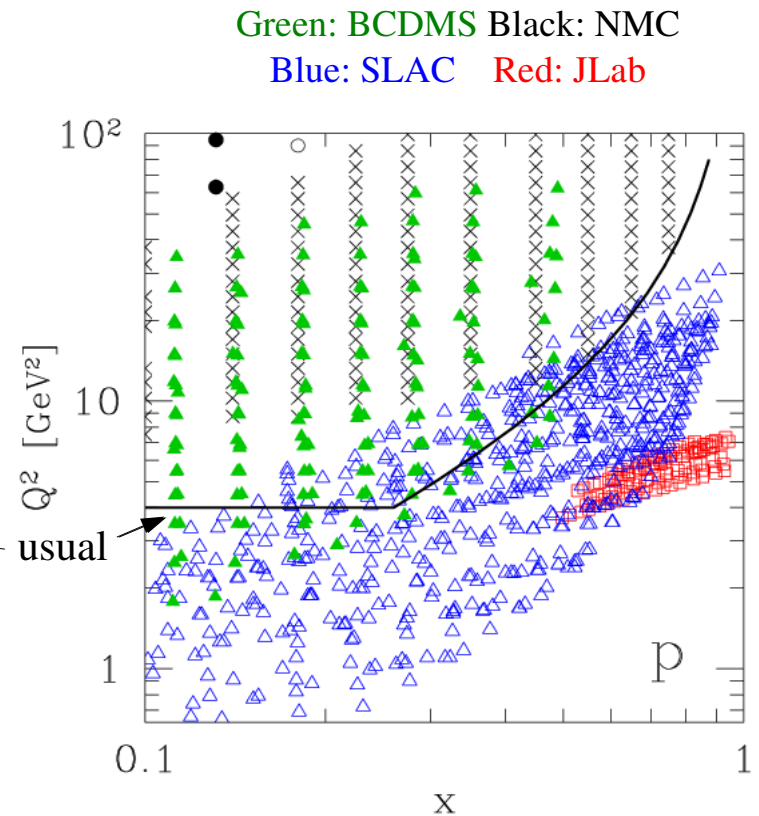
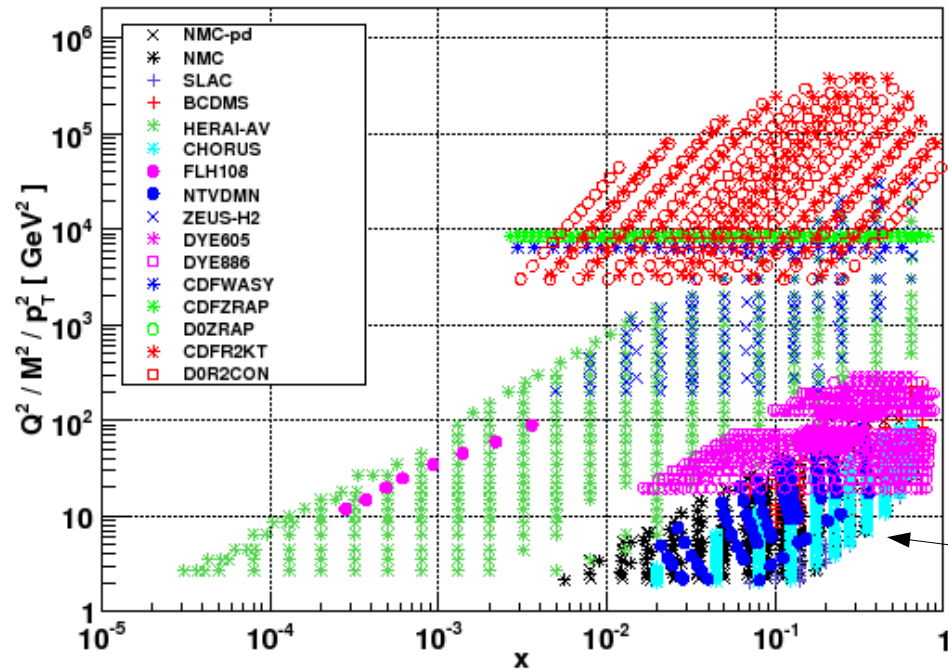
PDFs

$F_2(n)$

$W, Z / W', Z', \text{Higgs}$
(or any other “hard” observable)

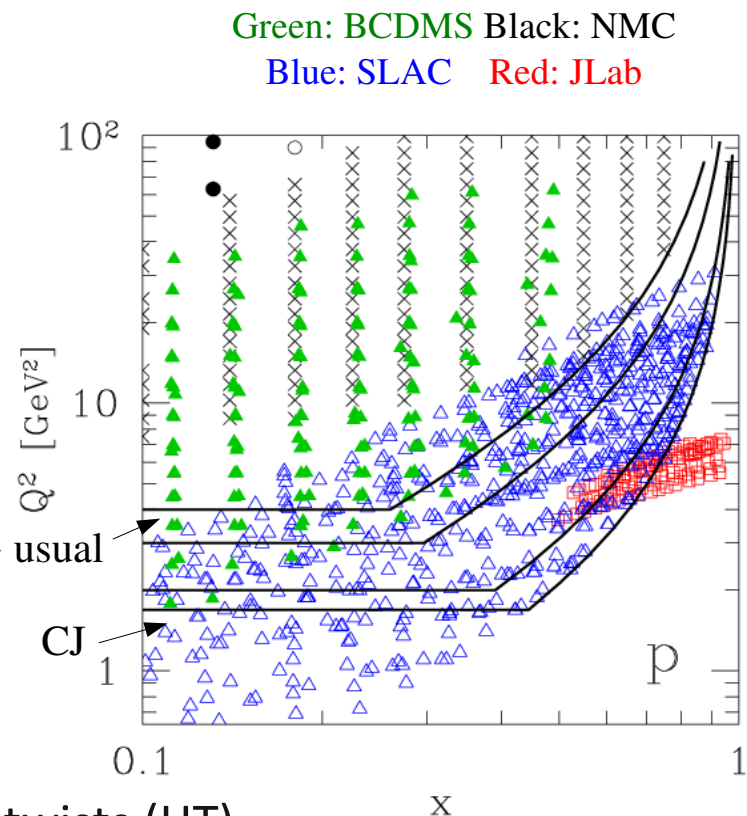
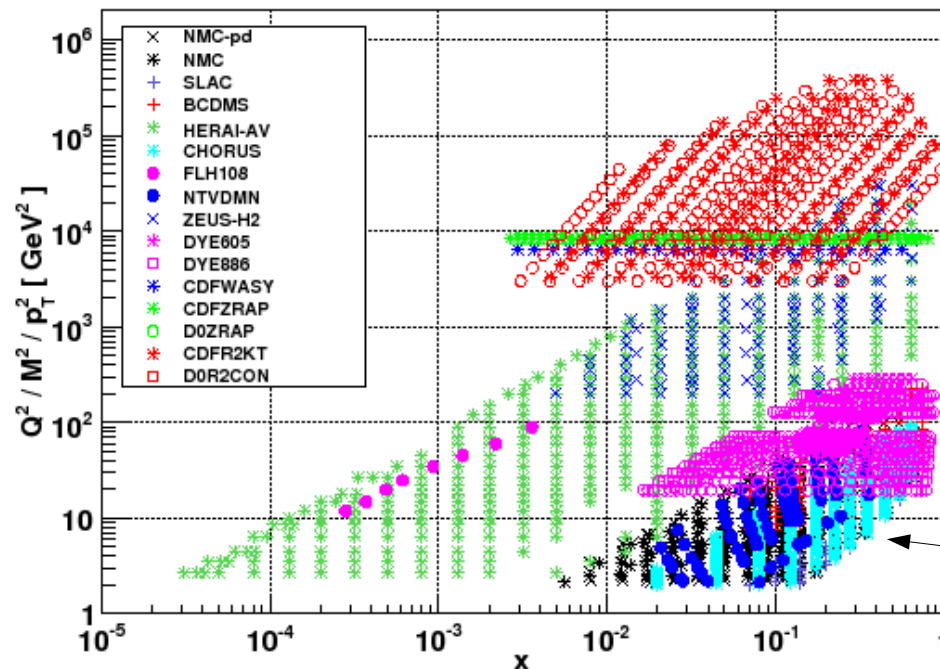
Large-x, small- Q^2 corrections

NNPDF2.0 dataset



Large-x, small- Q^2 corrections

NNPDF2.0 dataset



1/ Q^{2n} suppressed:

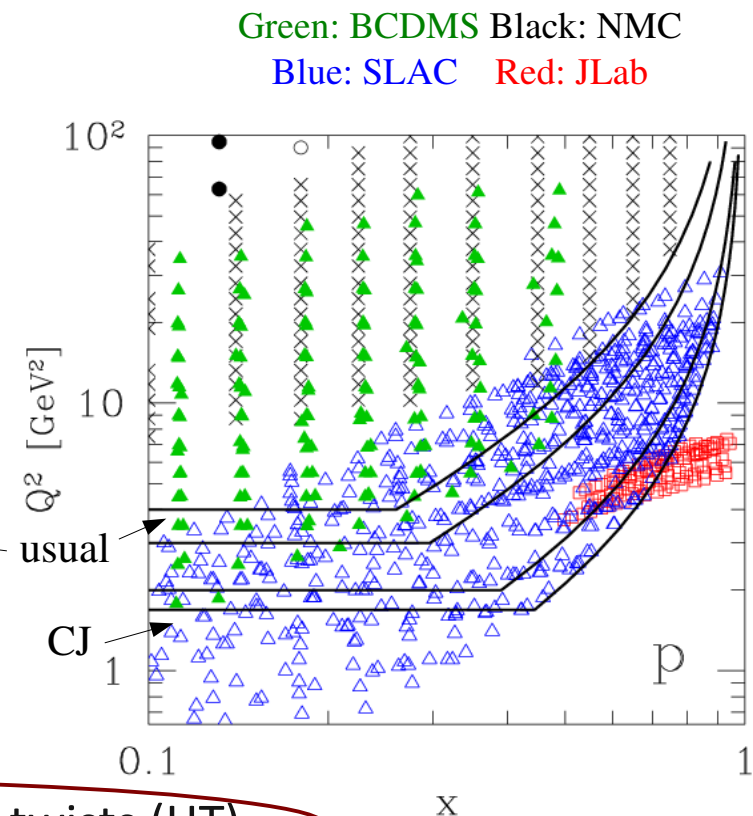
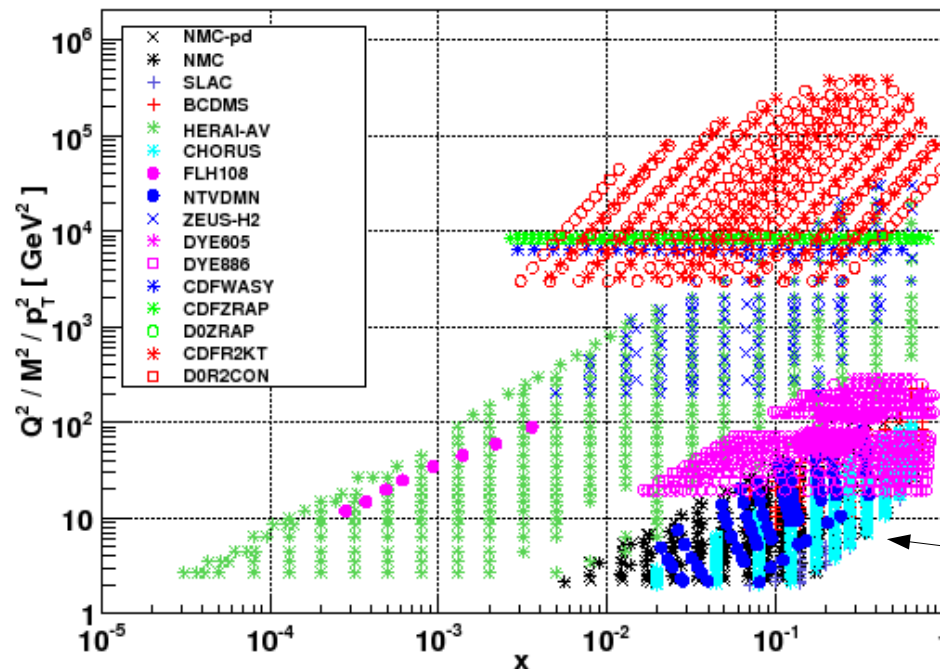
- Target mass corrections (TMC), higher-twists (HT)
- Current jet mass, quark mass, large-x QCD evolution

Non-suppressed

- Nuclear corrections, threshold resum., parton recomb.

Large-x, small- Q^2 corrections

NNPDF2.0 dataset



1/ Q^{2n} suppressed:

- Target mass corrections (TMC), higher-twists (HT)
- Current jet mass, quark mass, large-x QCD evol.

Non-suppressed

- Nuclear corrections, threshold resum., parton recomb.

included in CJ fits

CJ fits: results in a nutshell

summary: Accardi, MENU2010 proceedings

□ Standard cuts:

- PDF insensitive to TMC, HT
- Nuclear corrections not negligible (but usually neglected...)

□ Looser kinematic cuts

- PDFs stable as cut is varied about the largest allowed
- Substantial reduction in “experimental” PDF errors

□ Stability w.r.t. TMCs

Brady, Accardi, Hobbs, Melnitchouk, PRD 84, 074008 (2011)

- The fitted HT term compensates for differences in TMC models
 - Leading-twist PDFs have little systematic error (good!)
 - HT term has $\approx 50\%$ uncert. (not so good, if you care for this...)

CJ fits: results in a nutshell

summary: Accardi, MENU2010 proceedings

□ Standard cuts:

- PDF insensitive to TMC, HT
- Nuclear corrections not negligible (but usually neglected...)

□ Looser kinematic cuts

- PDFs stable as cut is varied about the largest allowed
- Substantial reduction in “experimental” PDF errors

□ Stability w.r.t. TMCs

Brady, Accardi, Hobbs, Melnitchouk, PRD 84, 074008 (2011)

- The fitted HT term compensates for differences in TMC models
 - Leading-twist PDFs have little systematic error (good!)
 - HT term has $\approx 50\%$ uncert. (not so good, if you care for this...)

□ New d -quark parametrization

- Dramatic increase in d PDF in $x \rightarrow 1$ limit

□ Large sensitivity to nuclear model

**...but large theoretical
uncertainties
(CJ11)**

Nuclear corrections - theoretical uncertainty

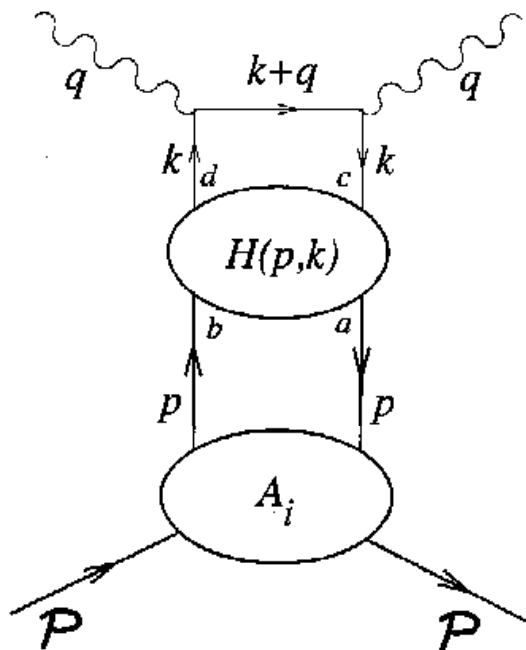
$$F_{2d}(x_B, Q^2) = \int_{x_B}^A dy \mathcal{S}_A(y, \gamma) F_2^{TMC+HT}(x_B/y, Q^2) \left(1 + \frac{\delta^{off} F_2(x)}{F_2(x)} \right)$$

Free nucleon str.fn.

“Smearing function”

Calculated from nuclear wave-function:

- CD-Bonn
 - AV18
 - WJC-2
 - WJC-1
- } non-relativistic
- } relativistic



Off-shell correction

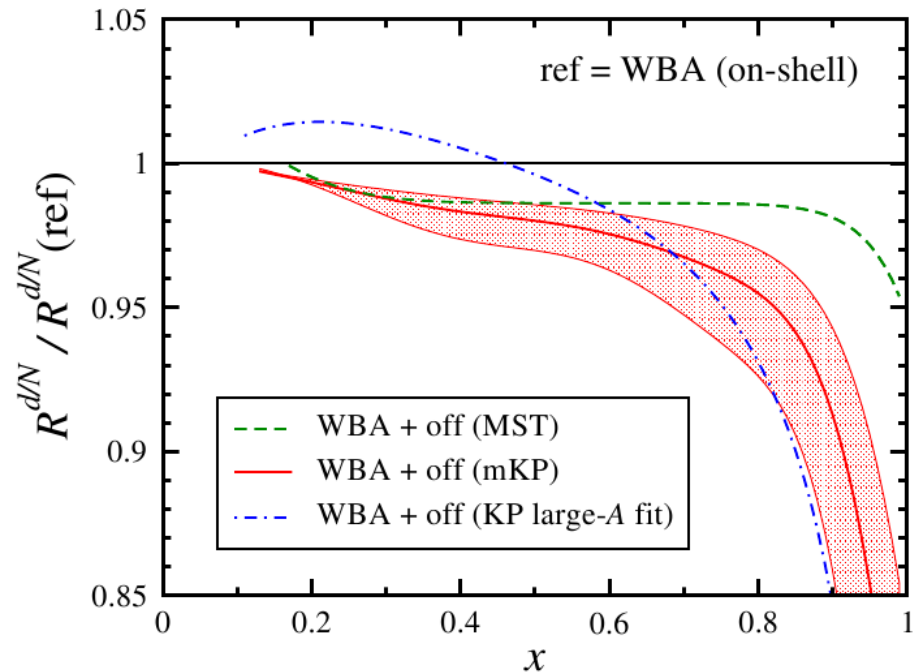
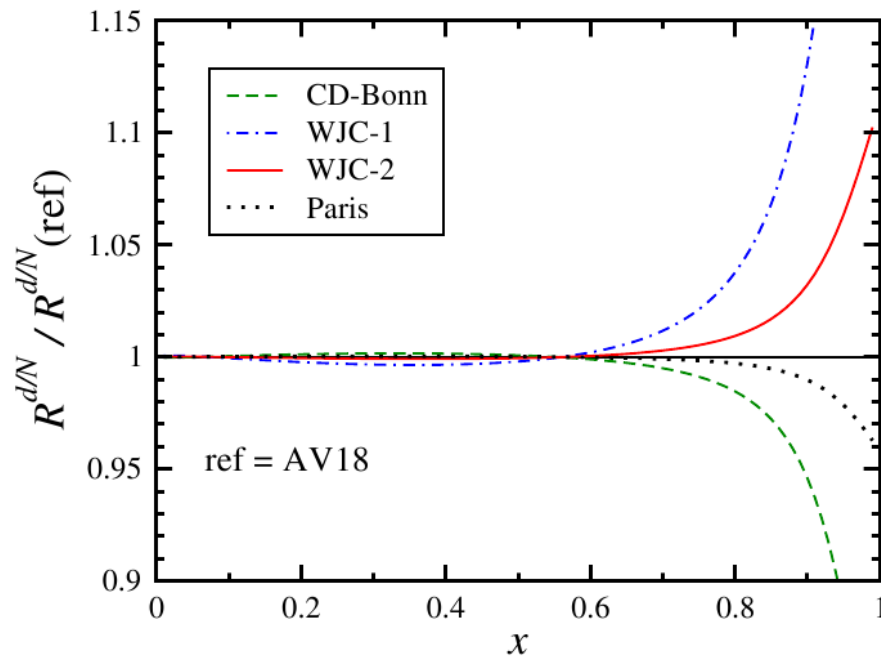
Models (little theory guidance):

- Melnitchouk & C. (MST)
- Kulagin-Petti (KP) fits of A/d ratios
- modified KP model

Nuclear corrections - theoretical uncertainty

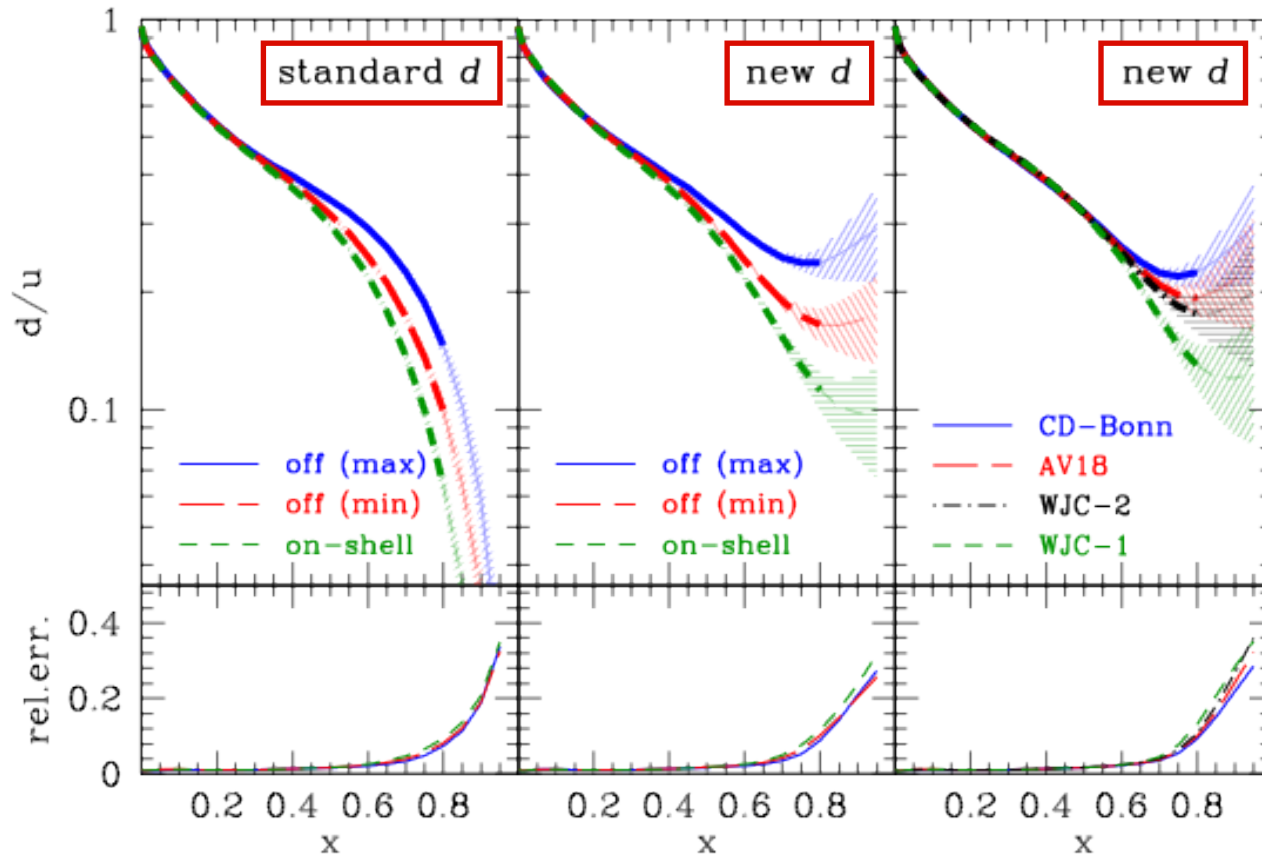
$$F_{2d}(x_B, Q^2) = \int_{x_B}^A dy \mathcal{S}_A(y, \gamma) F_2^{TMC+HT}(x_B/y, Q^2) \left(1 + \frac{\delta^{off} F_2(x)}{F_2(x)} \right)$$

Free nucleon str.fn.



CJ fits: effect of d -quark parametrization

Accardi et al. PRD 84, 014008 (2011)

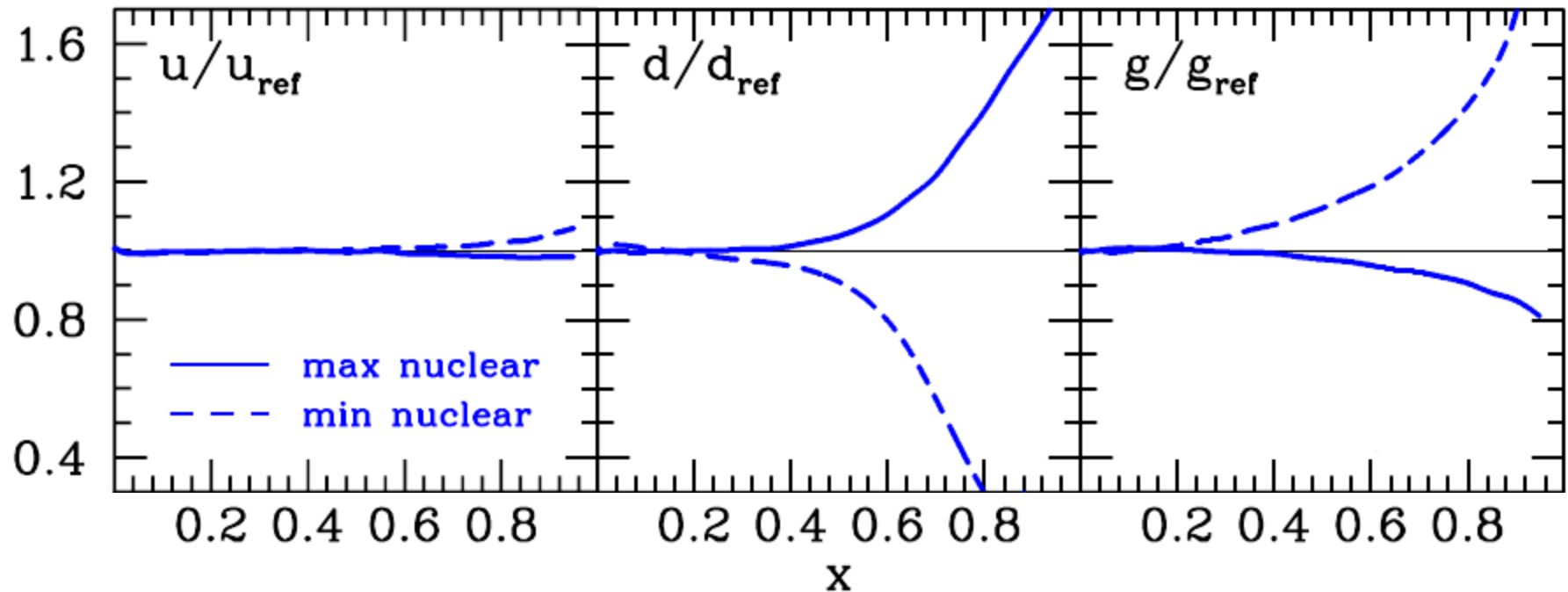


- Dramatic increase in d PDF in $x \rightarrow 1$ limit with more flexible parametrization

$$d'(x) = d(x) + \alpha x^\beta u(x)$$

CJ fits: nuclear model systematic error

Accardi et al. PRD 84, 014008 (2011)



Large sensitivity to nuclear corrections model

- *d-quarks*: directly, due to corrections applied to $F_2(d)$
- *gluons*: due to correlations induced by jet data

Application:
The d/u ratio at $x \rightarrow 1$

PDF fitting and neutron $F_2(n)$

data

- DIS: p, **deuteron**
- $p+p(\text{pbar}) \rightarrow l^+l^-, W^\pm$
- $p+p(\text{pbar}) \rightarrow \text{jets}, \gamma+\text{jet}$

theory

- pQCD at NLO
- Factorization & universality
- Large- x , low- Q^2 , **nuclear corr.**

fits

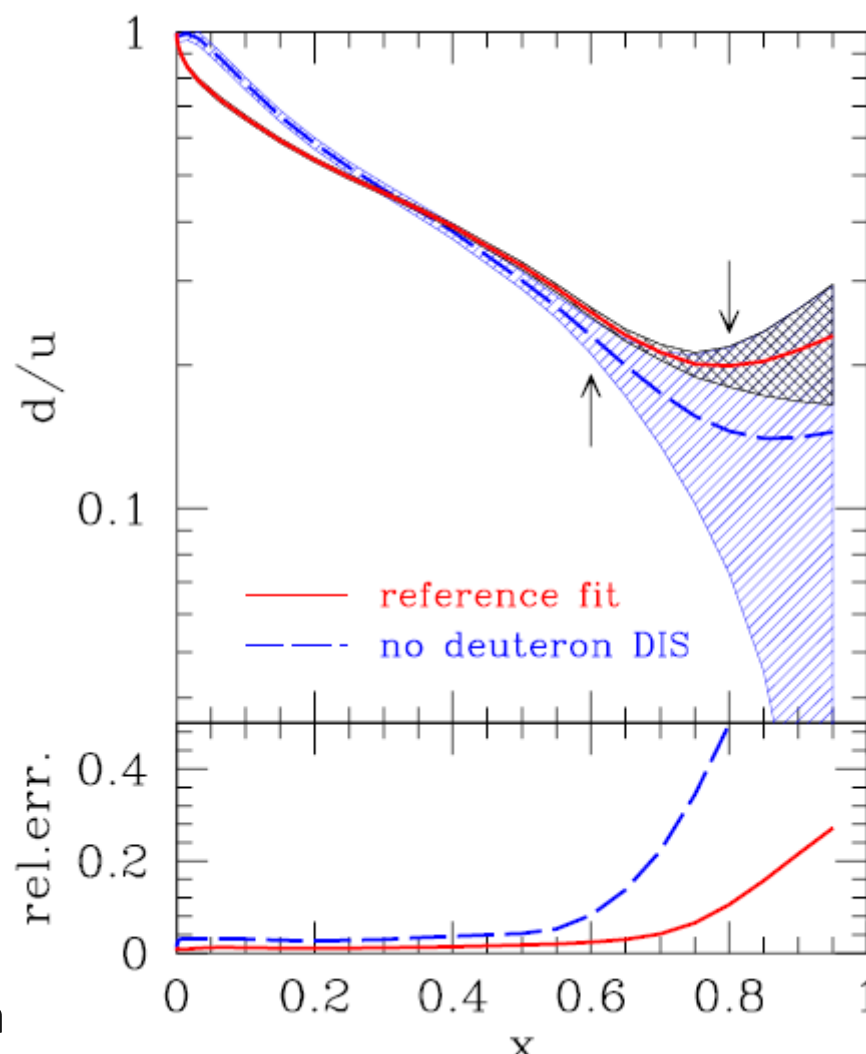
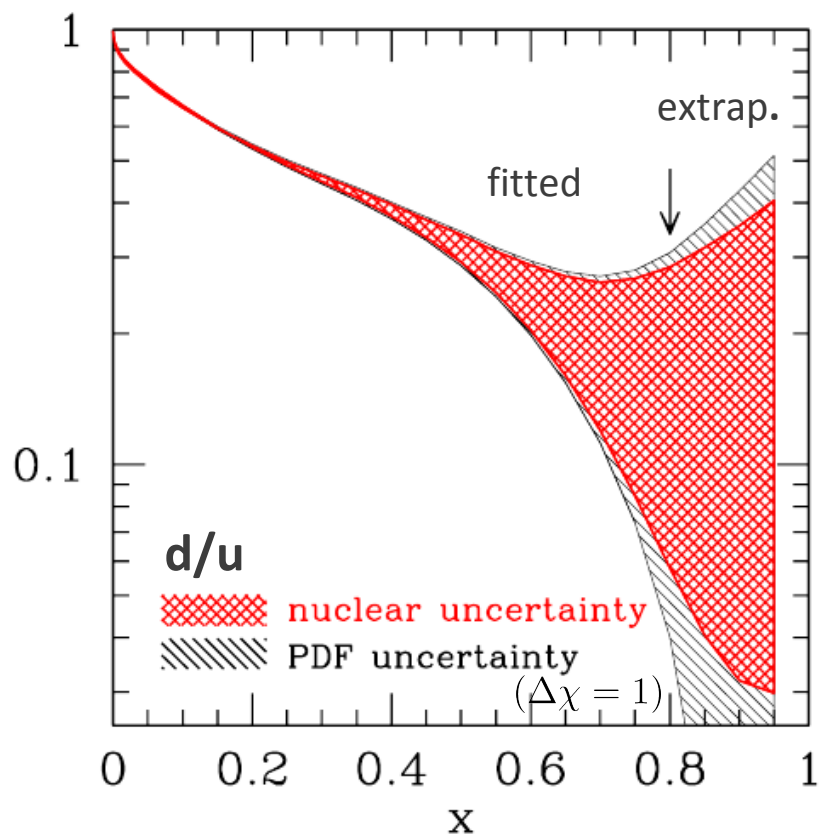
- Parametrize PDF at Q_0 , evolve to Q
- Minimize χ^2

PDFs

Extrapolate d/u to $x \rightarrow 1$
Extract $F_2(n)$ from data

The CTEQ-JLab d/u

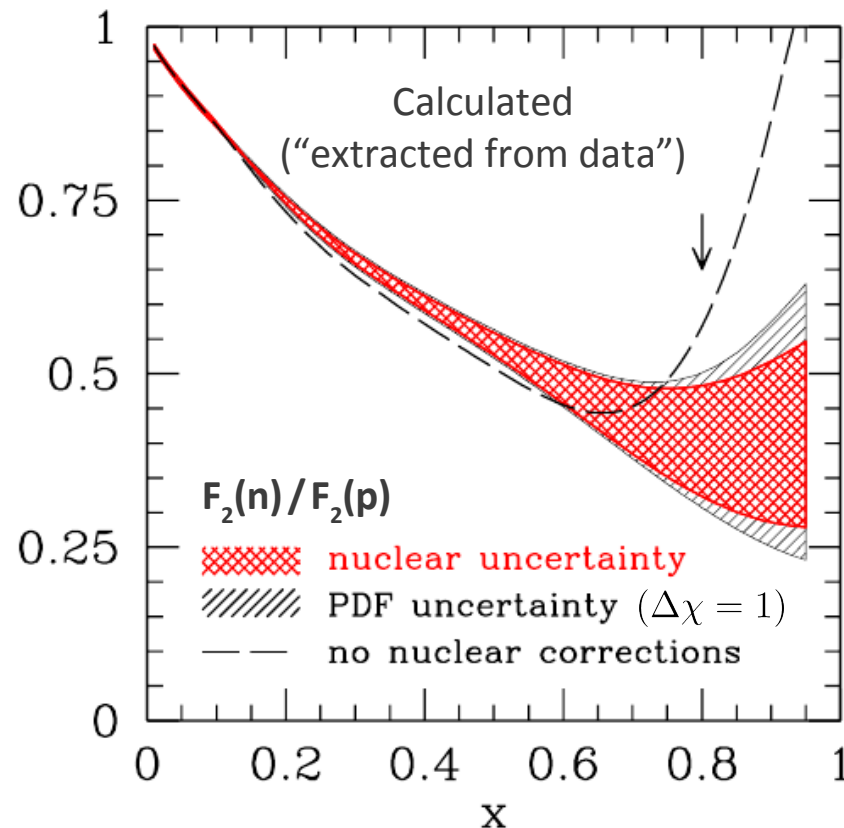
Accardi et al. PRD 84, 014008 (2011)



- ❑ Nuclear uncertainty eats away improved statistics from low- W^2 data

The CTEQ-JLab $F_2(n) / F_2(p)$

Accardi et al. PRD 84, 014008 (2011)



- Well behaved extrapolation for each nuclear model
 - however, beware of PDF “parametrization bias”
- But: **large nuclear uncertainty** (covers all theory predictions)

Constraining nuclear corrections

Need data to constrain nuclear corrections!

□ Data minimally sensitive to nuclear corrections

- DIS with slow spectator proton (BONUS, BONUS12)
 - Quasi-free neutrons
- DIS with fast spectator (DeepX)
 - Off-shell neutrons – but large, poorly controlled FSI
- $^3\text{He}/^3\text{H}$ ratios (MARATHON)

JLab

□ Data on free (anti)protons, sensitive to d or g

- $e+p: F_L$, parity-violating DIS **JLab, HERA** (e^+p vs. e^-p)
- $\nu+p, \bar{\nu}+p$ **Minerva ???**
- $p+p, p+\bar{p}$ at large positive rapidity **Tevatron, LHC**
 - W charge asymmetry, Z rapidity distribution **RHIC ??**

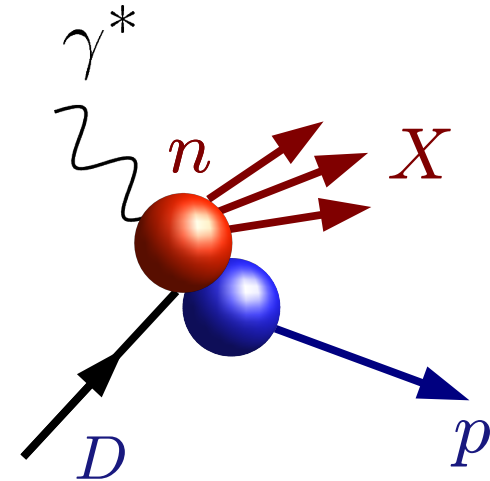
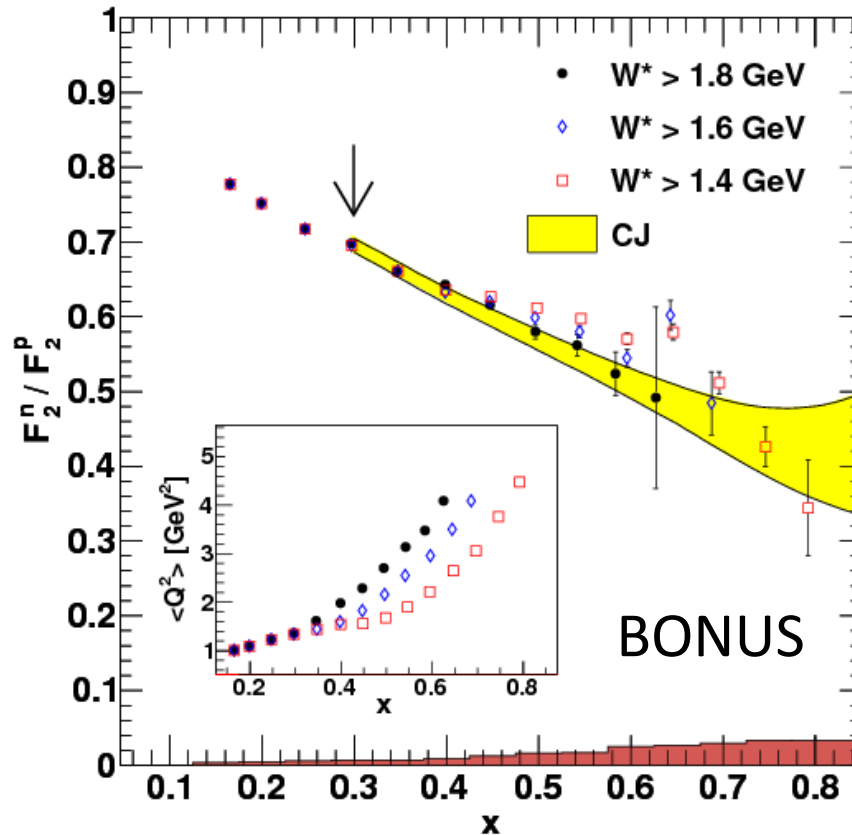
□ Cross-talk data

- $p+d$ at large negative rapidity – dileptons; maybe W, Z ?
 - Sensitive to nuclear corrections, cross-checks $e+d$

RHIC ??

Quasi-free neutrons from BONUS

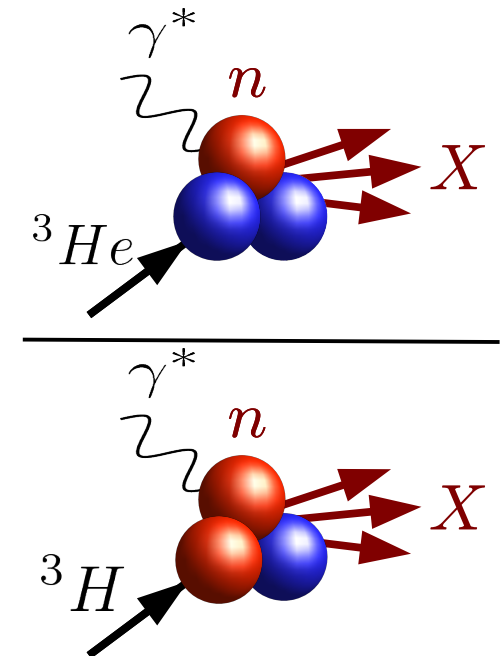
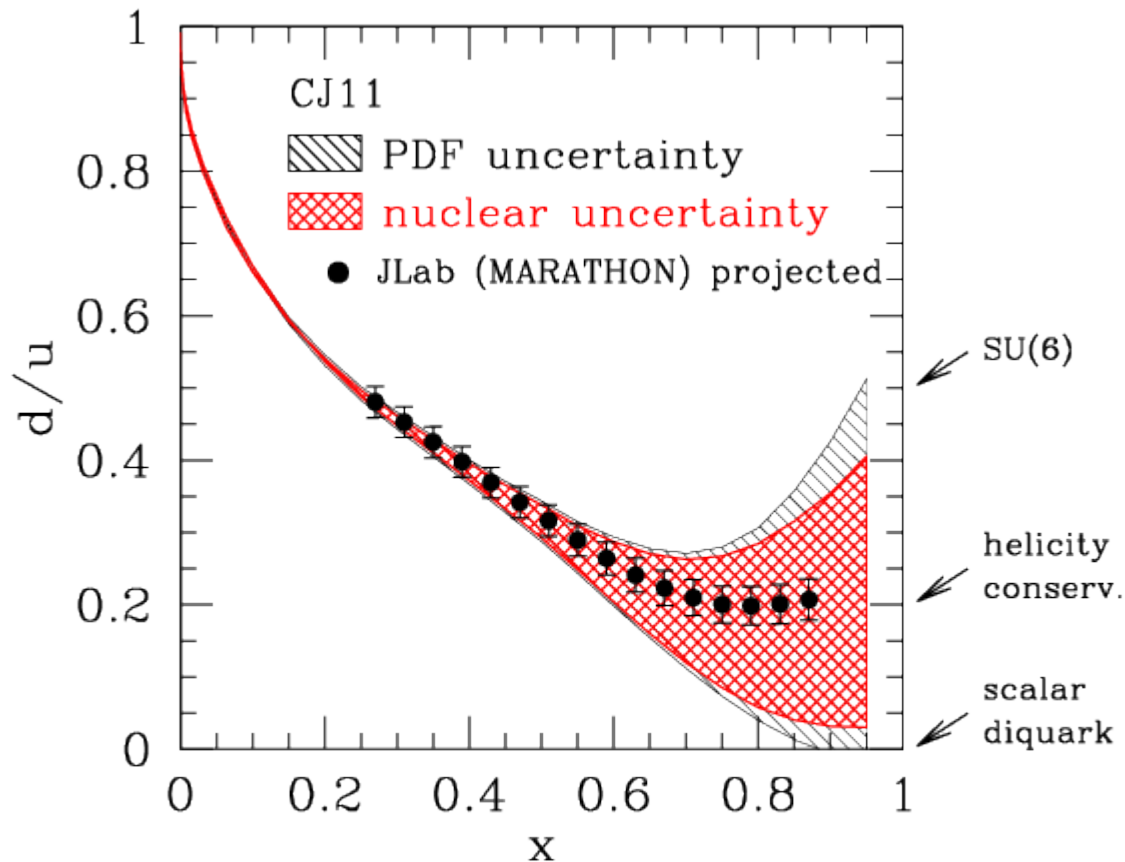
N.Baillie et al., arXiv:1110.2770



- DIS data (black disks) too uncertain at $x > 0.5$
 - Need to wait for BONUS12 / MARATHON

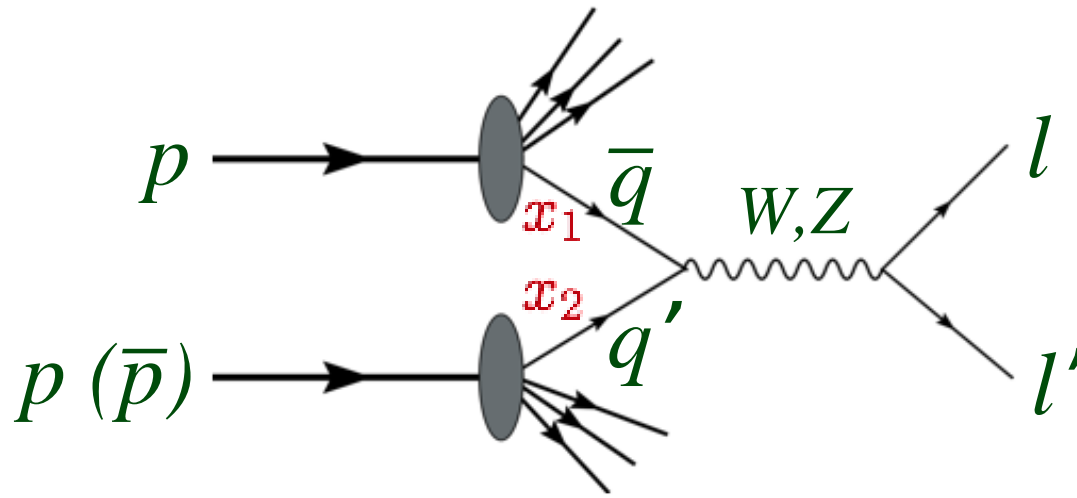
Quasi-free neutrons from MARATHON

Approved JLAB12 experiment



□ Nuclear corrections largely cancel in the ratio fo $^3\text{He}/^3\text{H}$ cross sections

W,Z production



□ Example: W and decay lepton charge asymmetry at large rapidity

$$A_W(y) = \frac{\sigma(W^+) - \sigma(W^-)}{\sigma(W^+) + \sigma(W^-)} \approx \frac{d/u(x_2) - d/u(x_1)}{d/u(x_2) + d/u(x_1)} \quad [x_1 \gg x_2]$$

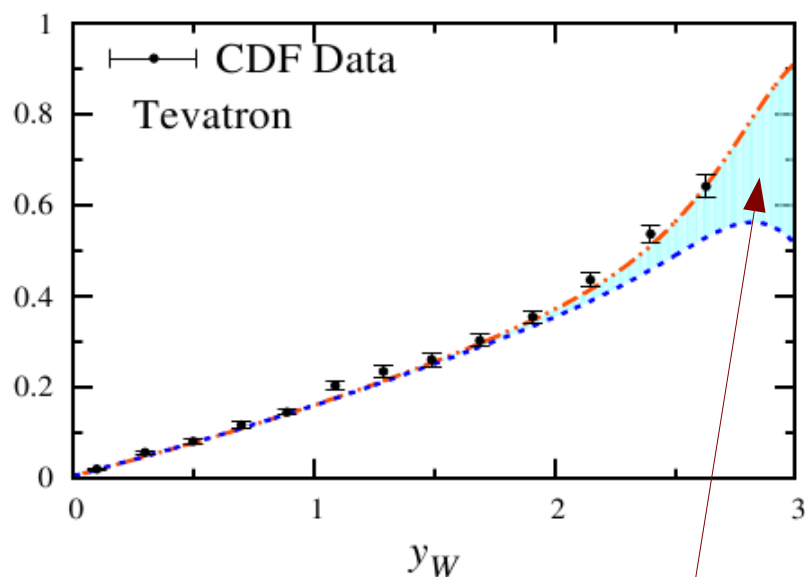
$$A_l(y) = A_W \otimes B_{W \rightarrow l}(y)$$

W charge asymmetry at Tevatron

Brady, Accardi, Melnitchouk, Owens, *arXiv:1110.5398, JHEP*

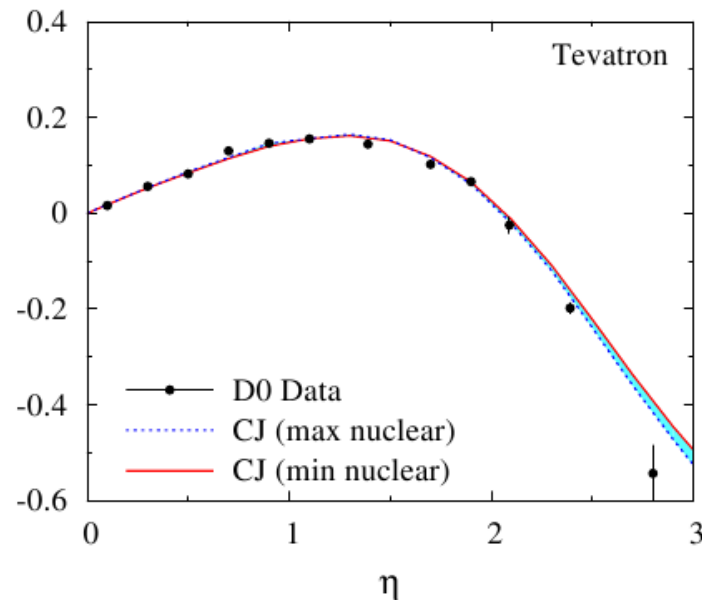
Directly reconstructed W:

- highest sensitivity to large x



From decay lepton $W \rightarrow l + \nu$:

- smearing in x



sensitive to
 d at high x

Can constrain
Nuclear models!

❑ Too little large- x sensitivity in lepton asymmetry:

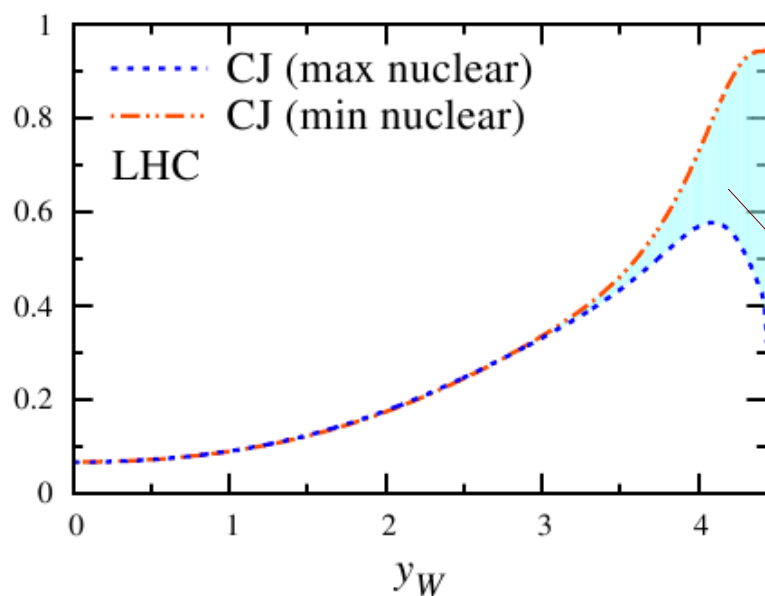
— need reconstructed W

W charge asymmetry at LHC

Brady, Accardi, Melnitchouk, Owens, arXiv:1110.5398, JHEP

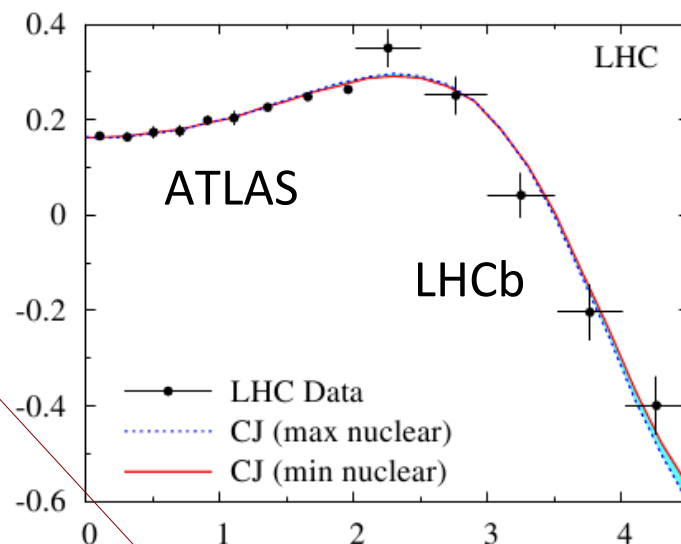
Directly reconstructed W:

- highest sensitivity to large x



From decay lepton $W \rightarrow l + \nu$:

- smearing in x



❑ Would be nice to reconstruct W at LHCb

- Needs more statistics
- Systematics in W reconstruction?
- Is it at all possible?? (too many holes in detector)

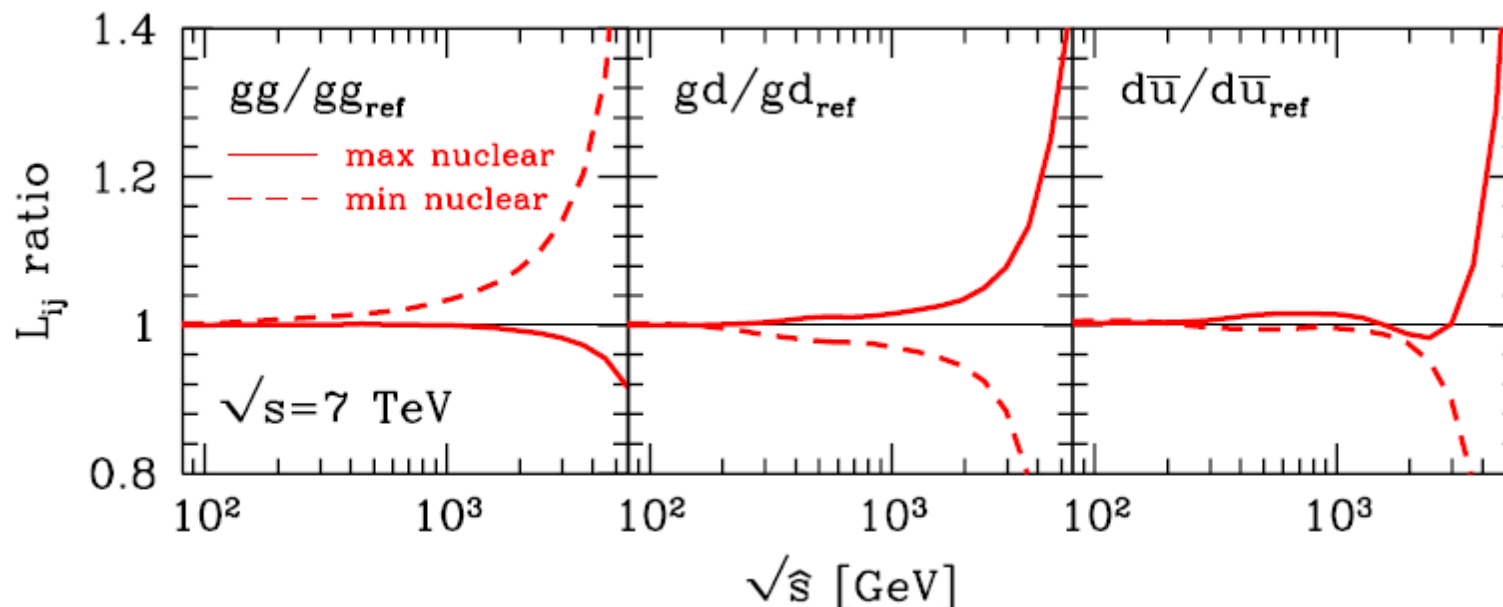
Can constrain
Nuclear models!

Parton luminosity at colliders

Accardi et al. PRD 84, 014008 (2011)

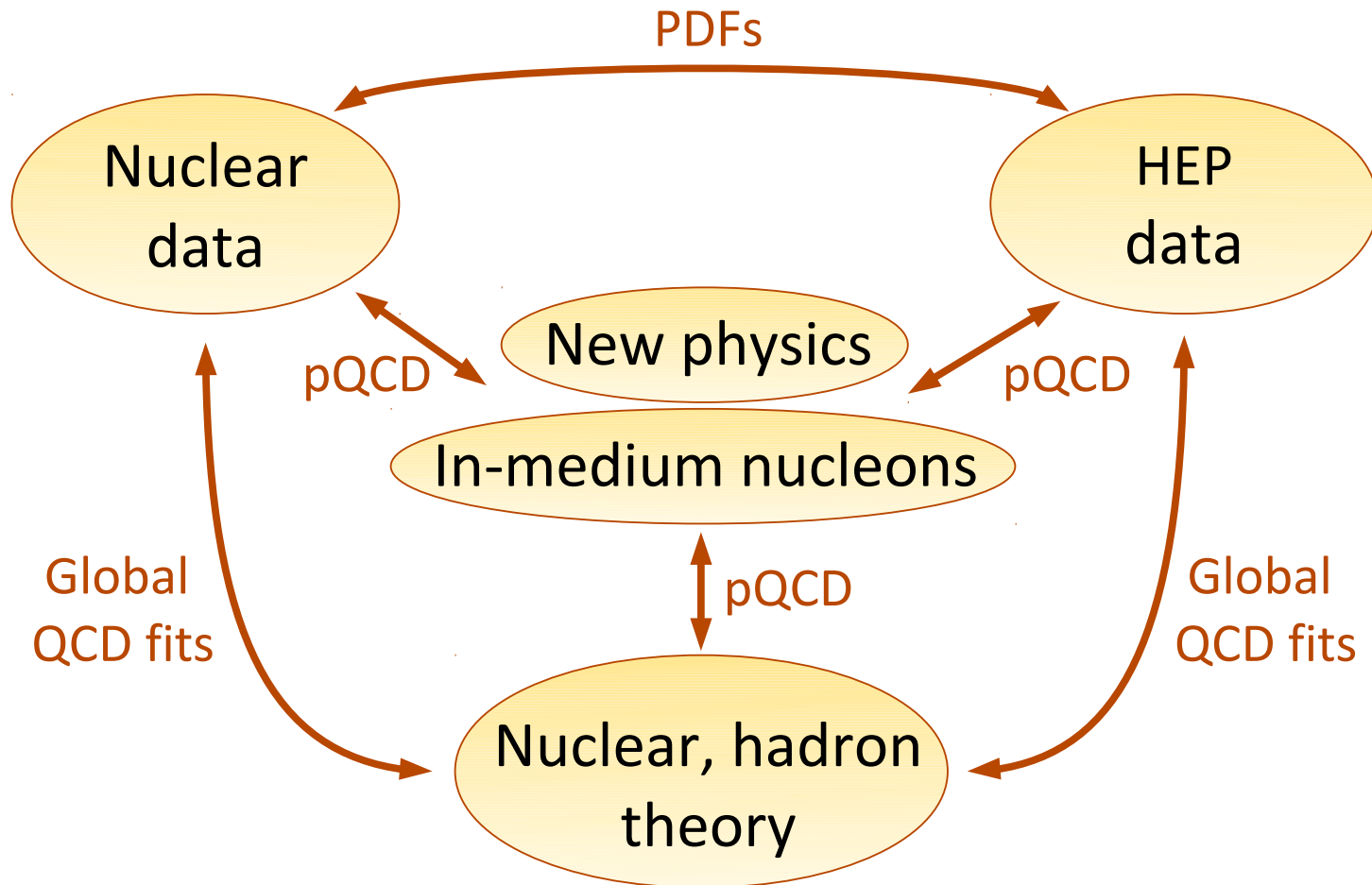
- Large- x PDF uncertainties affect total cross sections for objects of large mass $\hat{s} = (p_1 + p_2)^2 = x_1 x_2 s$ (or large rapidity $x_{1,2} = \sqrt{\hat{s}/s} e^{\pm y}$)

$$L_{ij} = \frac{1}{s(1 + \delta_{ij})} \left[\int_{\hat{s}/s}^1 \frac{dx}{x} f_i(x, \hat{s}) f_j\left(\frac{\hat{s}}{xs}, \hat{s}\right) + (i \leftrightarrow j) \right]$$



Summary

- Ongoing CTEQ-JLab global fits attacking large- x PDFs:
 - integrate across hadronic physics, connect with rest of subatomic physics



Plans

□ In preparation / near future

- Fits with latest data (HERA, large-x DIS cross sections, LHC @ 7 TeV)
- Correlated errors where available; tensions between data sets
- Public release of PDF + error sets (and accompanying sfw)
- LHC / RHIC phenomenology; will be ready for JLab 12 GeV, E906, ...

□ Longer term

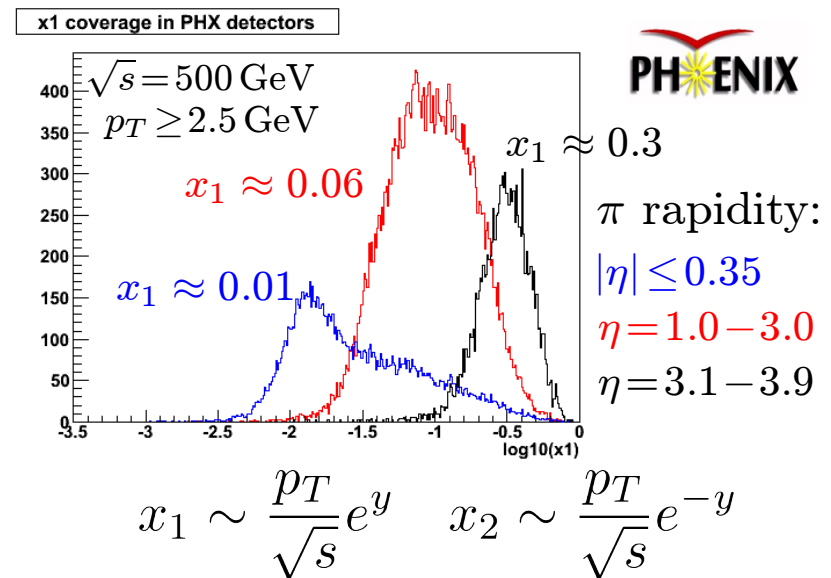
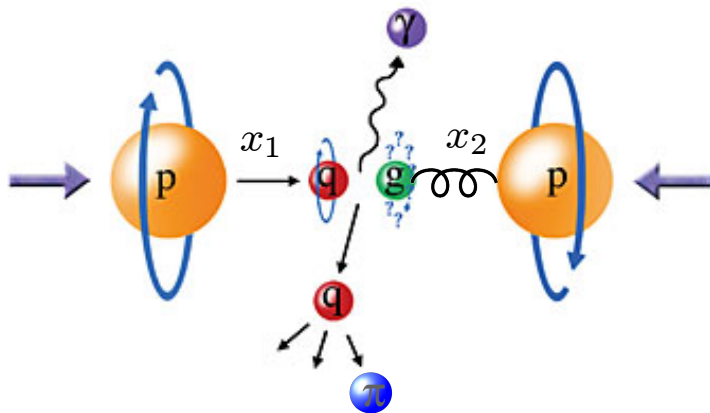
- F_L / σ data on deuterium (large-x gluons); heavy quarks
- large-x resummation, jet mass corrections, quark-hadron duality
- better off-shell corrections, extend to gluons

Backup slides

Small x gluons at colliders: hadronic structure

- Gluon spin at small x at RHIC requires particle production at large y

$$\sigma(\vec{p}\vec{p} \rightarrow \pi^0 X) \propto \Delta q(x_1) \Delta g(x_2) \hat{\sigma}^{qg \rightarrow qg} D_q^{\pi^0}(z)$$



- Precise large-x PDFs needed:
 - to measure smallest-x gluon helicity

Valence quarks at large x

□ d/u quark ratio particularly sensitive to quark dynamics in nucleon

□ **SU(6) spin-flavor symmetry**

– proton wave function

$$p^\uparrow = -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1 \\ + \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0$$

interacting
quark

spectator
diquark

diquark spin

Valence quarks at large x

□ d/u quark ratio particularly sensitive to quark dynamics in nucleon

□ **SU(6) spin-flavor symmetry**

– proton wave function

$$p^\uparrow = -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1 \\ + \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0$$

– 50% $(qq)_1$ 50% $(qq)_0$, $u = 2d$ at all x

$$\frac{d}{u} = \frac{1}{2} \implies \frac{F_2^n}{F_2^p} = \frac{2}{3}$$

Valence quarks at large x

□ Broken SU(6) : scalar diquark dominance

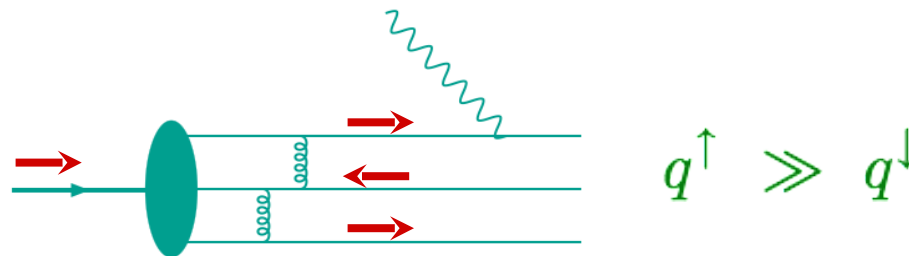
- $M_{\Delta} > M_N \Rightarrow (qq)_1$ has larger energy than $(qq)_0$
- But only u quark couples to scalar diquark:

$$\frac{d}{u} \rightarrow 0 \quad \Rightarrow \quad \frac{F_2^n}{F_2^p} \rightarrow \frac{1}{4}$$

*Feynman 1972, Close 1973
Close/Thomas 1988*

□ Broken SU(6) : hard gluon exchange

- helicity of struck quark = helicity of struck hadron



$$\frac{d}{u} \rightarrow \frac{1}{5} \quad \Rightarrow \quad \frac{F_2^n}{F_2^p} \rightarrow \frac{3}{7}$$


Farrar, Jackson, 1975

The mKP off-shell nucleon model

Accardi et al. PRD 84, 014008 (2011)

- Nucleon at large x = valence quark + spectator diquark


$$q_v(x, p^2) = \int ds \int_{-\infty}^{k_{\max}^2} dk^2 D_{q/N}(s, k^2, x, p^2)$$



Nucleon virtuality diquark
inv. mass squared Quark virtuality

- Quark spectral function, with spectator diquark

$$D_{q/N} \approx \delta(s - s_0) \Phi(k^2, \Lambda(p^2)) \quad [s_0 = 2.1 \text{ GeV}^2 \text{ from fits}]$$



Cutoff scale

- Physical interpretation: nucleon size changes with p^2 : $R_N \sim 1/\Lambda$

Valence quarks at large x

□ Broken SU(6) : scalar diquark dominance

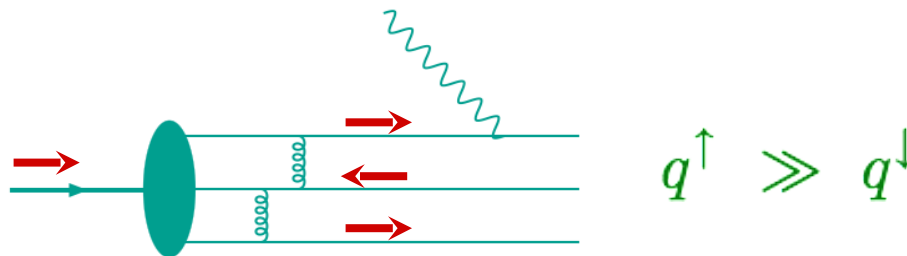
- $M_{\Delta} > M_N \Rightarrow (qq)_1$ has larger energy than $(qq)_0$
- But only u quark couples to scalar diquark:

$$\frac{d}{u} \rightarrow 0 \quad \Rightarrow \quad \frac{F_2^n}{F_2^p} \rightarrow \frac{1}{4}$$

*Feynman 1972, Close 1973
Close/Thomas 1988*

□ Broken SU(6) : hard gluon exchange

- helicity of struck quark = helicity of struck hadron



$$\frac{d}{u} \rightarrow \frac{1}{5} \quad \Rightarrow \quad \frac{F_2^n}{F_2^p} \rightarrow \frac{3}{7}$$

Farrar, Jackson, 1975

The mKP off-shell nucleon model

Accardi et al. PRD 84, 014008 (2011)

- Expand $F_2(N)$ to first order in virtuality:

$$F_2^N(x, Q^2, p^2) = F_2^N(x, Q^2) \left(1 + \delta f_2(x, Q^2) \frac{p^2 - M^2}{M^2} \right)$$

- In the mKP model

$$\delta f_2 = c + \frac{\partial \log q_v}{\partial x} x(1-x) \frac{(1-\lambda)(1-x)M^2 + \lambda s_0}{(1-x)^2 M^2 - s_0}$$

- Only 1 free parameter

$$\lambda = \left. \partial \log \Lambda^2 / \partial \log p^2 \right|_{p^2=M^2} = -2(\delta R_N / R_N)(\delta p^2 / M^2)$$

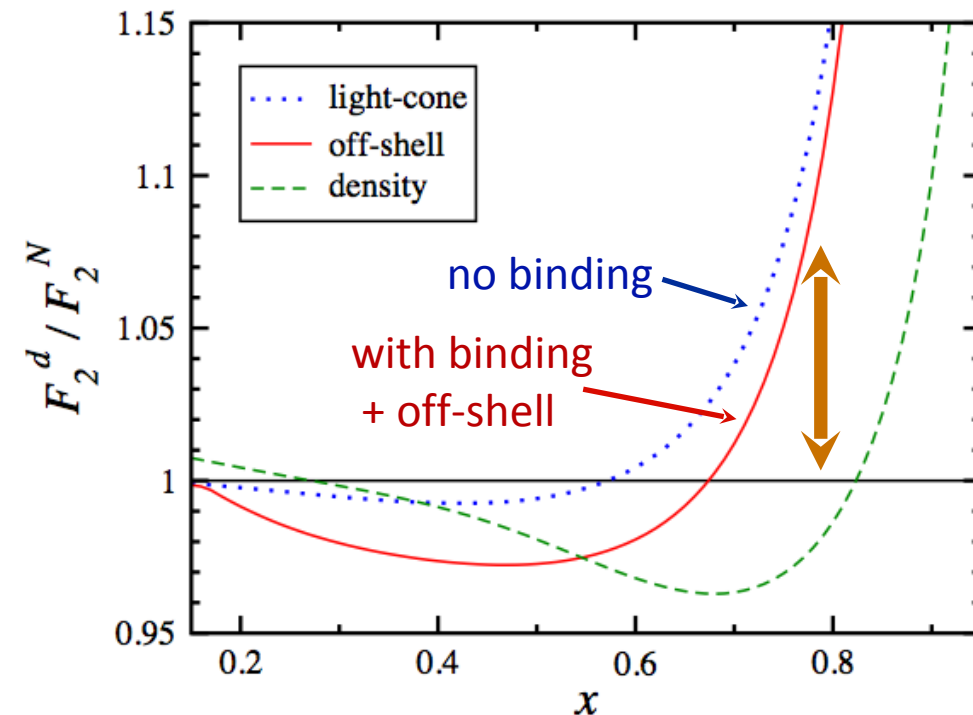
Physical interpretation:
nucleon size changes with p^2 : $R_N \sim 1/\Lambda$

$$\delta p^2 = \langle p^2 - M^2 \rangle$$

$$\int d^4 p (p^2 - M^2) \mathcal{S}_d(y)$$

Nuclear corrections

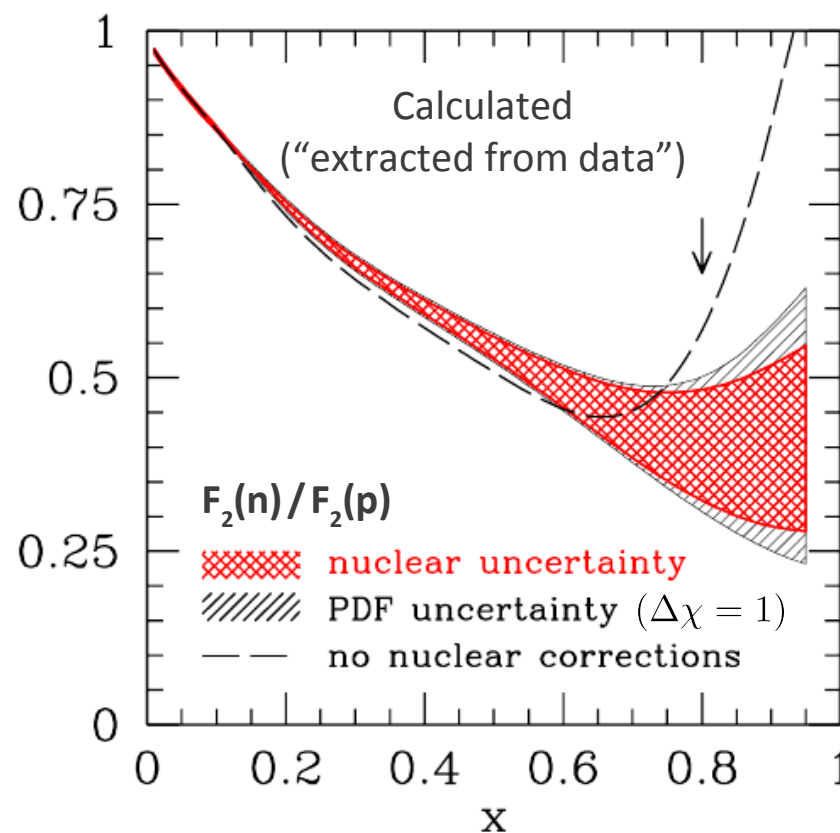
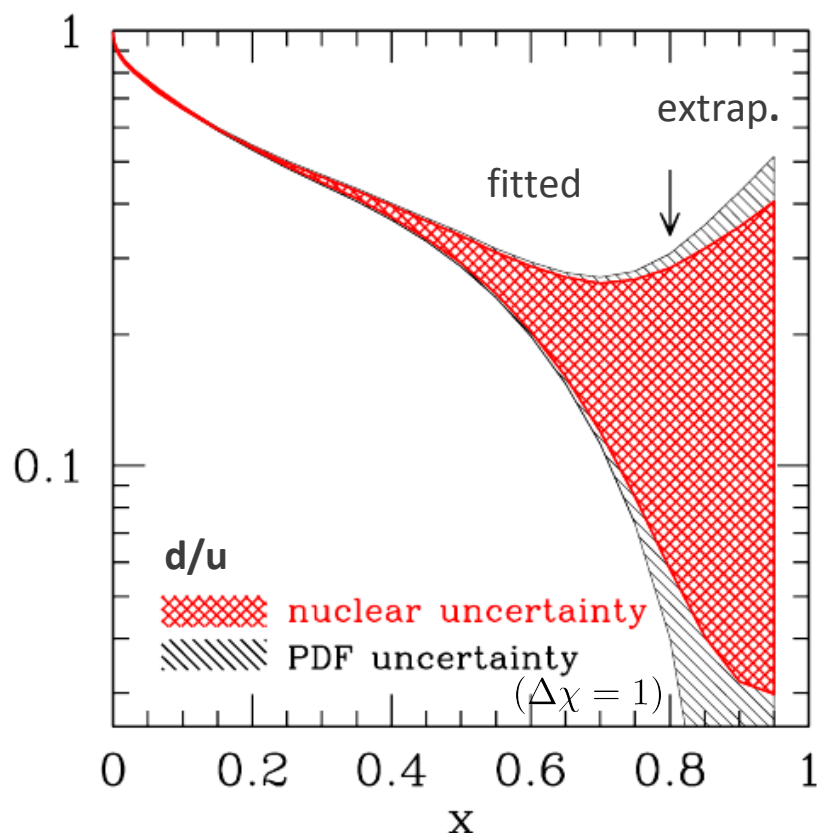
$$F_{2d}(x_B, Q^2) = \int_{x_B}^A dy \mathcal{S}_A(y, \gamma) F_2^{TMC+HT}(x_B/y, Q^2) \left(1 + \frac{\delta^{off} F_2(x)}{F_2(x)} \right)$$



- Using off-shell model, obtains *larger neutron* (larger d) than light-cone model
- But smaller *neutron* (larger d) than no nuclear effects or density model

The CTEQ-JLab d/u and $F_2(n)$

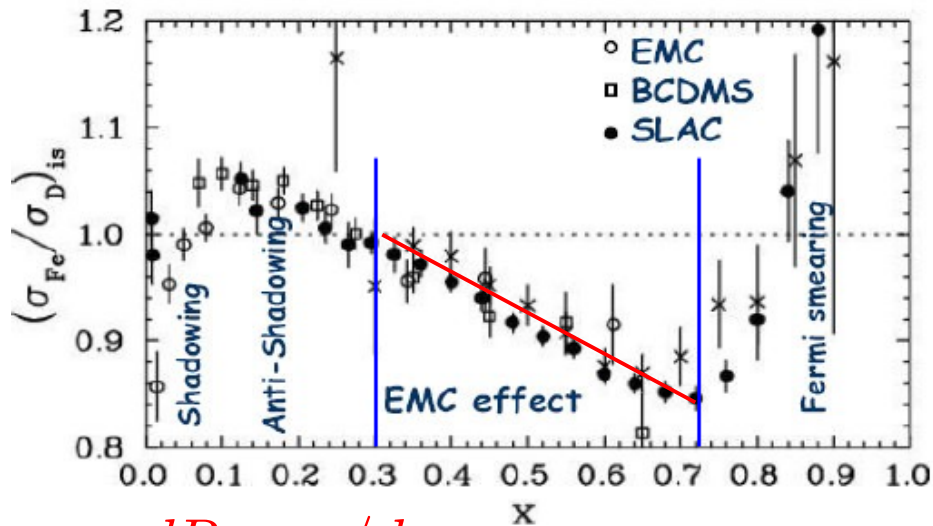
Accardi et al. PRD 84, 014008 (2011)



- Well behaved extrapolation for each nuclear model
 - however, beware of PDF "parametrization bias"
- But: **large nuclear uncertainty** (covers all theory predictions)

In the meantime... look at $x > 1$

DIS at $x < 1$: partonic structure of hadrons



$$dR_{EMC}/dx$$

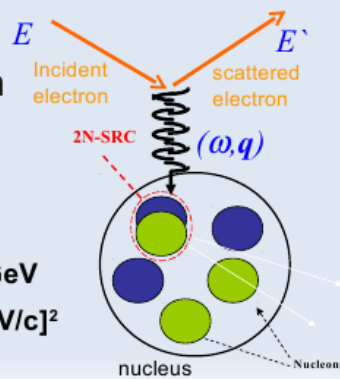
X_B counts the number of nucleons involved in the reaction

→ for $X_B > j$, at least j nucleons are involved in the reaction

$E, E' \text{ 3 - 5 GeV}$

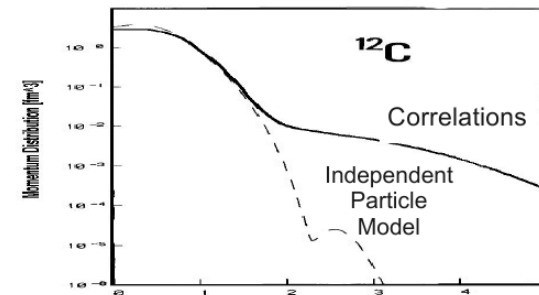
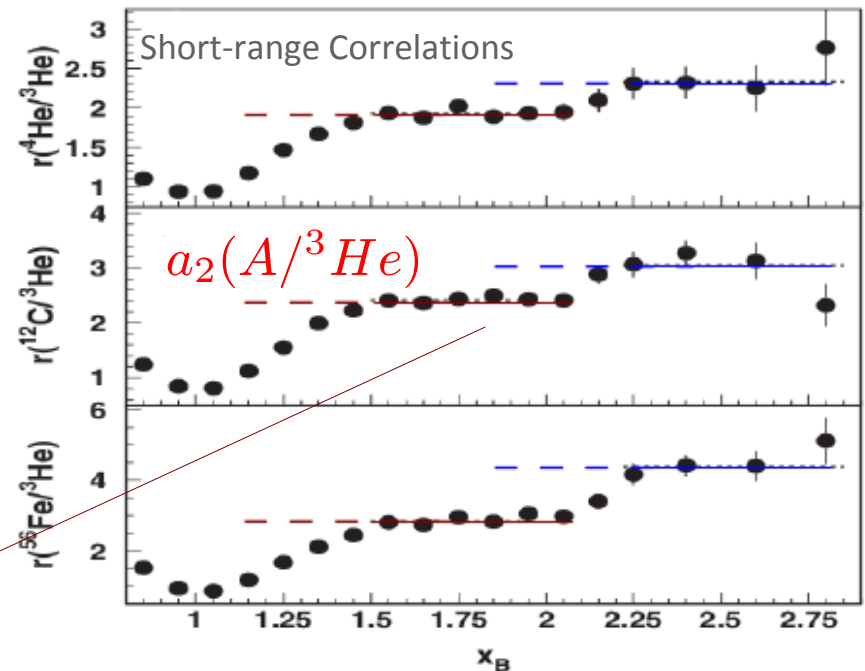
Kinematical regime: $Q^2 \text{ 2 - 3 [GeV/c]}^2$

$0 \leq X_B \leq A$



Inelastic at $x > 1$:

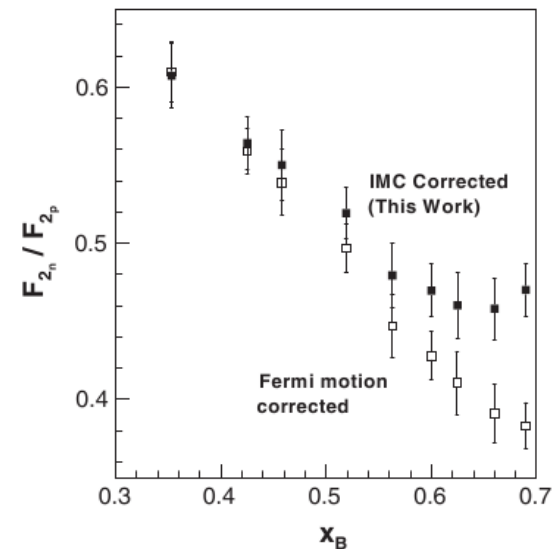
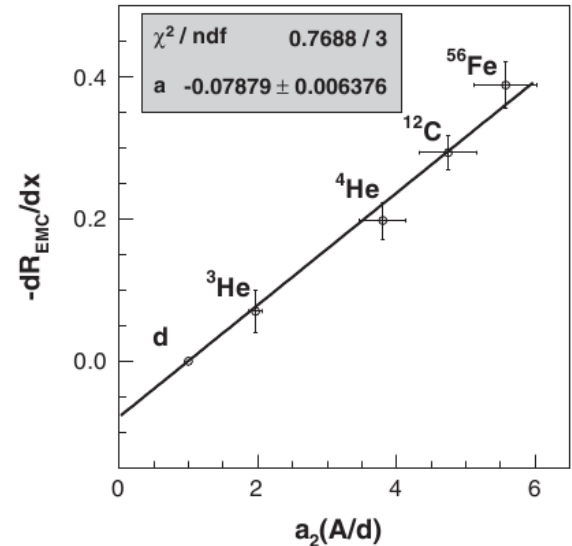
nucleonic structure of nuclei



SRC/EMC correlation

Weinstein et al., PRL 106 (2011) 052301

- There is a definite correlation
- Why? Speculations...
 - Hard tail of nuclear w.f. shifts strength to higher x
 - Parton structure modified by short-range interaction
 - ...
- Will be studied experimentally
 - e.g., is the EMC effect different when tagging a fast spectator?
 - the faster the more off-shell: p^2 dependence?
- Extrapolate to deuterium, extract $F_2(n)$



IMC constraints on deuteron corrections

Hen, Accardi, Melnitchouk, Piasetzky, PRC 2012

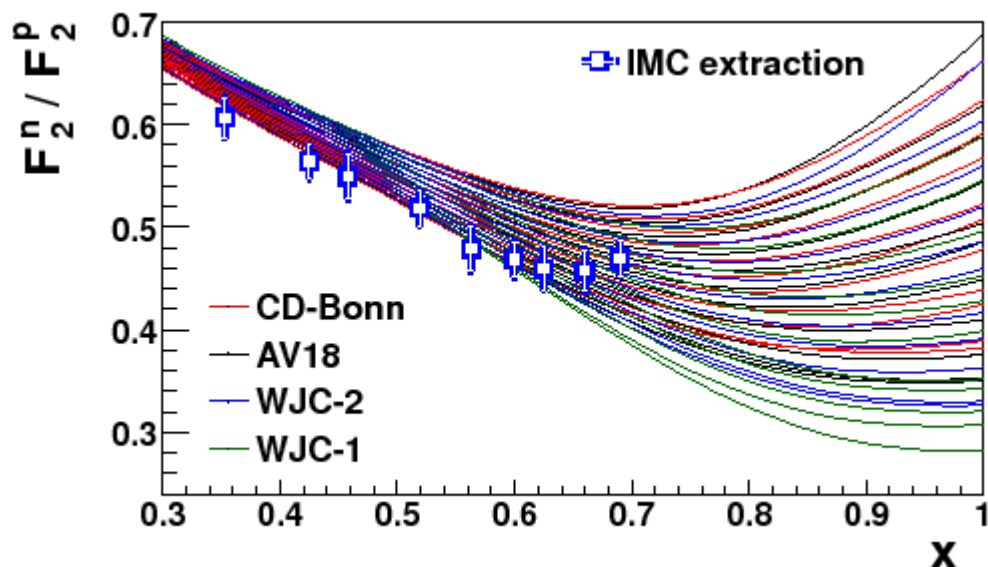
- 4 wave-functions, 1 free off-shell parameter each

$$\lambda_{off} = -2 \frac{\delta R}{R} \frac{\delta p^2}{p^2}$$

Bound nucleon swelling:

- model (Close et al. 1985) $\sim 1.2\%$
- fits: 0–3% range

Average nucleon virtuality,
fixed by wave-function choice

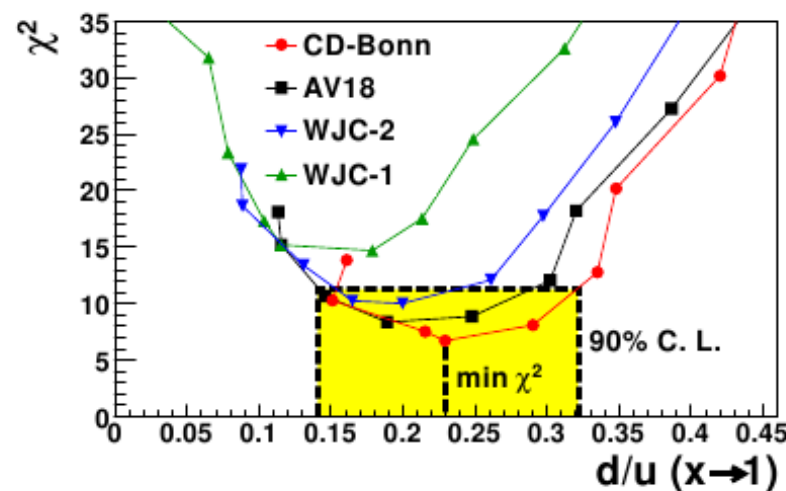
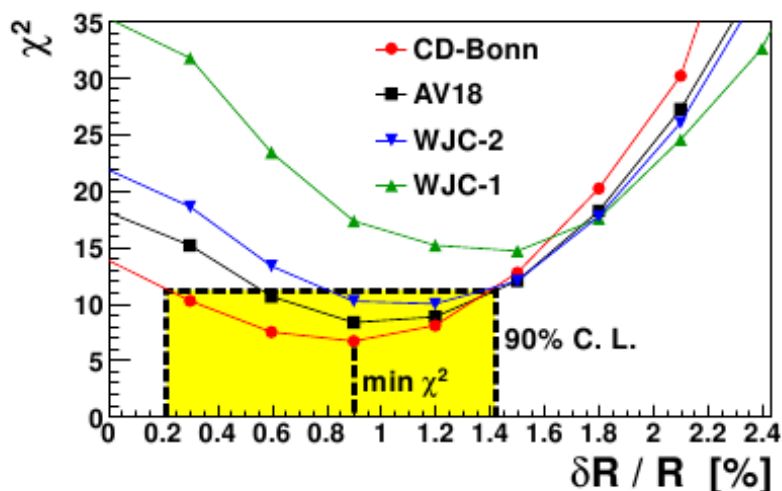


IMC constraints on deuteron corrections

Hen, Accardi, Melnitchouk, Piasezky, PRC to appear

IMC extracted data constrains nuclear model, and d/u ratio

- Treat choice of w.f. as a (continuous) free parameter



- Clearly indicates mild to medium off-shell corrections

$$\delta R/R = 0.2\% - 1.4\%$$

- Disfavors hard wave-functions such as WJC-1

- Excludes models based on
 - SU(6) symmetry
 - Scalar di-quark dominance

$$d/u \rightarrow 0.23 \pm 0.09$$

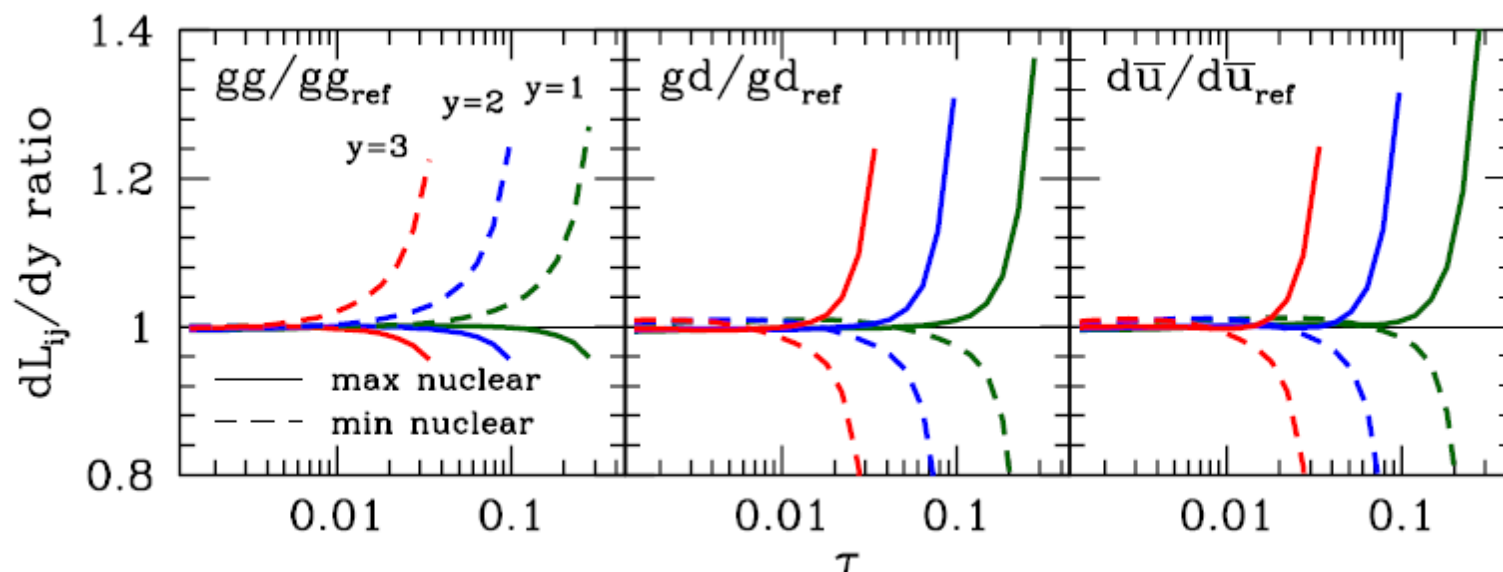
Parton luminosities

Accardi et al. PRD 84, 014008 (2011)

□ ... or large rapidity:

$$\frac{dL_{ij}}{dy} = \frac{1}{s(1 + \delta_{ij})} \left[f_i(\tau e^y, \hat{s}) f_j(\tau e^{-y}, \hat{s}) + (i \leftrightarrow j) \right]$$

$x_{1,2} = \tau e^{\pm y} \quad \tau = \sqrt{\hat{s}/s}$



(Note: ratios are largely independent of s)